



GCSE

Mathematics (9-1)

Unit J560/04: Paper 4 (Higher Tier)

General Certificate of Secondary Education

Mark Scheme for November 2018

OCR (Oxford Cambridge and RSA) is a leading UK awarding body, providing a wide range of qualifications to meet the needs of candidates of all ages and abilities. OCR qualifications include AS/A Levels, Diplomas, GCSEs, Cambridge Nationals, Cambridge Technicals, Functional Skills, Key Skills, Entry Level qualifications, NVQs and vocational qualifications in areas such as IT, business, languages, teaching/training, administration and secretarial skills.

It is also responsible for developing new specifications to meet national requirements and the needs of students and teachers. OCR is a not-for-profit organisation; any surplus made is invested back into the establishment to help towards the development of qualifications and support, which keep pace with the changing needs of today's society.

This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

© OCR 2018

Annotations used in the detailed Mark Scheme.

Annotation	Meaning
\checkmark	Correct
×	Incorrect
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working (after correct answer obtained), provided method has been completed
MO	Method mark awarded 0
M1	Method mark awarded 1
M2	Method mark awarded 2
A1	Accuracy mark awarded 1
B1	Independent mark awarded 1
B2	Independent mark awarded 2
MR	Misread
SC	Special case
Λ	Omission sign

These should be used whenever appropriate during your marking.

The **M**, **A**, **B** etc. annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate these scripts to show how the marks have been awarded.

It is not mandatory to use annotations for any other marking, though you may wish to use them in some circumstances.

Subject-Specific Marking Instructions

- M marks are for <u>using a correct method</u> and are not lost for purely numerical errors.
 A marks are for an <u>accurate</u> answer and depend on preceding M (method) marks. Therefore MO A1 cannot be awarded.
 B marks are <u>independent</u> of M (method) marks and are for a correct final answer, a partially correct answer, or a correct intermediate stage.
 SC marks are for <u>special cases</u> that are worthy of some credit.
- 2 Unless the answer and marks columns of the mark scheme specify **M** and **A** marks etc., or the mark scheme is 'banded', then if the correct answer is clearly given and is <u>not from wrong working</u> **full marks** should be awarded.

Do <u>not</u> award the marks if the answer was obtained from an incorrect method, i.e. incorrect working is seen <u>and</u> the correct answer clearly follows from it.

3 Where follow through (**FT**) is indicated in the mark scheme, marks can be awarded where the candidate's work follows correctly from a previous answer whether or not it was correct.

Figures or expressions that are being followed through are sometimes encompassed by single quotation marks after the word *their* for clarity, e.g. FT 180 × (*their* '37' + 16), or FT 300 – $\sqrt{(their '5^2 + 7^2')}$. Answers to part questions which are being followed through are indicated by e.g. FT 3 × *their* (a).

For questions with FT available you must ensure that you refer back to the relevant previous answer. You may find it easier to mark these questions candidate by candidate rather than question by question.

- 4 Where dependent (**dep**) marks are indicated in the mark scheme, you must check that the candidate has met all the criteria specified for the mark to be awarded.
- 5 The following abbreviations are commonly found in GCSE Mathematics mark schemes.
 - cao means correct answer only.
 - **figs 237**, for example, means any answer with only these digits. You should ignore leading or trailing zeros and any decimal point e.g. 237000, 2.37, 2.370, 0.00237 would be acceptable but 23070 or 2374 would not.
 - **isw** means **ignore subsequent working** (after correct answer obtained).
 - **nfww** means **not from wrong working**.
 - oe means or equivalent.
 - rot means rounded or truncated.
 - **seen** means that you should award the mark if that number/expression is seen anywhere in the answer space, including the answer line, even if it is not in the method leading to the final answer.
 - soi means seen or implied.
- 6 Make no deductions for wrong work after an acceptable answer unless the mark scheme says otherwise, indicated for example by the instruction 'mark final answer'.
- 7 As a general principle, if two or more methods are offered, mark only the method that leads to the answer on the answer line. If two (or more) answers are offered, mark the poorer (poorest).
- 8 When the data of a question is consistently misread in such a way as not to alter the nature or difficulty of the question, please follow the candidate's work and allow follow through for **A** and **B** marks. Deduct 1 mark from any **A** or **B** marks earned and record this by using the MR annotation. **M** marks are not deducted for misreads.

Mark Scheme

- 9 Unless the question asks for an answer to a specific degree of accuracy, always mark at the greatest number of significant figures even if this is rounded or truncated on the answer line. For example, an answer in the mark scheme is 15.75, which is seen in the working. The candidate then rounds or truncates this to 15.8, 15 or 16 on the answer line. Allow full marks for the 15.75.
- 10 If the correct answer is seen in the body and the answer given in the answer space is a clear transcription error allow full marks unless the mark scheme says 'mark final answer' or 'cao'. Place the annotation ✓ next to the correct answer.

If the answer space is blank but the correct answer is seen in the body allow full marks. Place the annotation \checkmark next to the correct answer.

If the correct answer is seen in the working but a completely different answer is seen in the answer space, then accuracy marks for the answer are lost. Method marks would still be awarded. Use the M0, M1, M2 annotations as appropriate and place the annotation × next to the wrong answer.

- 11 Ranges of answers given in the mark scheme are always inclusive.
- 12 For methods not provided for in the mark scheme give as far as possible equivalent marks for equivalent work. If in doubt, consult your Team Leader.
- 13 Anything in the mark scheme which is in square brackets [...] is not required for the mark to be earned, but if present it must be correct.

Question	Answer	Marks	Part marks a	nd guidance
1	8 cao	4	M3 for $\frac{their60 \times 2.25 - 125}{125}$ soi [0].08 or M2 for <i>their</i> 60 × 2.25 – 125 soi 10 or M1 for 60 × 2.25 soi 135	allow work in £ or p, alt method : M3 for $\frac{their60 \times 2.25}{125} - 1$ soi [0].08 or M2 for their 135 ÷ 125 soi by 1.08 or 108% or M1 for 60×2.25 soi 135 OR M3 for $\frac{2.25-their125+60}{their 125+60}$ soi[0].08 or M2 for 2.25 - their 125 ÷ 60 soi 0.16[6] or 0.17 or M1 for 125 ÷ 60 soi 2.08[3]

	Que	stion	Answer	Marks	Part marks a	nd guidance
2	(a)		a correct distance conversion e.g. 400 ÷ 1000 or [0].4 or 5 × 1000 or 5000	M1	accept any correct method	
			a scale factor e.g. 5[000] ÷ 400 soi figs 125 or 840 ÷ 66 soi 12.727… or 12.73 or figs 127	M 1		
			correct time conversion e.g. 14 × 60 or 840 or 66 ÷ 60 or 1[m] 6[s] or 1.1 or 825 ÷ 60	M 1		
			or 823 ± 60 correct figures e.g. 13.75 or 13.7 or 13.8 [14] 5.09 or 5.1 [5] 5090[] or 5100 5000 825 840 12.5 12.7 5.95 or 5.9 or 6 6.06 or 6.1	A1	Dep on M3	
	(b)		an acceptable response e.g. [he will not maintain this rate because] he will get tired	1		Accept any correct reason must not be contradicted.
3			an acceptable response e.g. it is not a right-angled triangle	1	Accept any correct response e.g. they should use the sine rule or cosine rule	

	Question	Answer	Marks	Part marks a	nd guidance
4		15.38 cao	6	M2 for 6400×1.025^8 oe soi 7797.78 orM1 for 1.025^k ($k>1$) oe soi 6724 ANDM2 for $6400 + 6400 \times [0].027 \times 8$ oe soi 7782.4 orM1 for $6400 \times [0].027$ oe soi 172.8 or 1382.4 ANDM1 for subtracting their two totals or their two interests e.g. their 7797.7785 their 7782.4 or their 1397.78 - their 1382.4	
5		28 or [£][0] .28	5	B1 for $7r + 15c = 7[00]$ or $[r =] c + [0.]12$ M1 for $7(c + [0.]12) + 15c = 7[00]$ or better oe or $r - c = [0.]12$ M1 for $7c + 84 + 15c = 7[00]$ or better oe or $7r - 7c = [0.]84$ M1 for $15c + 7c = 7[00] - [0.]84$ or better	Allow any pair of letters, see AG Trial-and-improvement will score 0 or 5 only allow work in pence or pounds i.e. removing brackets i.e. rearranging their equation
6		14.79 to 14.8	5	M2 for $\pi \times 12^2 \times 30$ soi by 13 564 to 13 574 or M1 for $\pi \times 12^2$ soi 452 to 453 B1 for $\frac{4}{3}\pi r^3$ = <i>their</i> 13 571 M1 for <i>their</i> 13 571 ÷ $\frac{4}{3}\pi$ or 3240	

	Que	stion	Answer	Marks	Part marks a	nd guidance
7	(a)		acceptable bisector of angle A with two pairs of supporting arcs	2	B1 for acceptable bisector of angle A with no or incorrect arcs	Tolerance ± 2° Use overlay
	(b)		acceptable perpendicular bisector of AC with supporting arcs	2	B1 for acceptable perpendicular bisector of AC with no or incorrect arcs	Tolerance ± 2 mm Use overlay
	(c)		their correct region shaded	1	Dep on at least (a) B1 and (b) B1	
8	(a)	(i)	13 860 000 oe	2	M1 for $2^5 \times 3^2 \times 5^4 \times 11 \times 7$ with at most one error	condone $2^5 \times 3^2 \times 5^4 \times 11 \times 7$ for 2 marks
		(ii)	$2^2 \times 3 \times 5 \times 11$ isw	2	M1 for answer one step away	
	(b)	(i)	2 × 3 ² × 5 ²	3	 B2 for answer one step away or a correct diagram e.g. factor tree or B1 for 2, 3 and 5 identified e.g. could be in a factor tree 	
		(ii)	90	3	M2 for [270 =] 2 × 3 × 3 × 3 × 5 oe or M1 for 2, 3 and 5 as factors of 270 or for an answer of 2, 3, 5, 6, 9, 10,15, 18, 30 or 45	Accept in factor tree or a division spine, allow M1 if one step away

	Question	Answer	Marks	Part marks a	nd guidance
9	(a)	% L p p 5 (19 (12 36) p)	3	B2 for three correct entries, ignore labels or B1 for one element in the correct place	
	(b)	$\frac{36}{72}$ oe	2	FT <i>their</i> labelled Venn diagram (2 sets) for 2 marks e.g. $\frac{their_{36}}{72}$ B1 for $\frac{k}{72}$ where k < 72	isw cancelling and conversion, accept 50% for 2 marks
10		-3 2	2	B1 for each	
11	(a)	7.5 oe	2	B1 for input to B as 19	Could be in diagram
	(b)	3(2x + 3) oe	2	B1 for output from A as $2x + 4$ oe	Could be in diagram
12		correct bar width and 'height' of 0.6	5	M2 for $15 \times 0.8 + 10 \times 0.9 + 15 \times 0.2$ or better e.g. $12 + 9 + 3$ or 24 or M1 for two correct frequencies calculated from 12, 9 and 3 AND M1 for $30 - their 24$ soi 6 M1 for <i>their</i> 6 ÷ 10 soi 0.6	
13		accept any correct answer e.g. he did not factorise fully [as 2 <i>x</i> is the full common factor]	1		

PMT

	Que	stion	Answer	Marks	Part marks a	nd guidance
14			$y = \frac{120}{\sqrt{x}}$ oe	3	M1 for $y = \frac{k}{\sqrt{x}}$ oe B1 for [<i>k</i> =] 120	e.g. condone $y = \frac{k}{\sqrt{9}}$ for M1
15	(a)		Correct box plot	2	B1 for at least 3 correct elements	See overlay
	(b)	(i)	Peter and has a larger median oe	1		Condone average for median
		(ii)	David and has a smaller IQR oe	1		Condone "neither as they have the same range"
16			(2x + 3)(x - 11) -1.5 oe 11	M2 B1	M1 for two brackets which give two correct terms correct or FT <i>their</i> two linear brackets	
17			[a=] 3 [b=] 4 [c=] -5	4	B2 for a = 3 or M1 for second differences = 6 M1 for revised terms of -1 3 7 11 or B1 for b = 4 or c = -5	
18			$y = -\frac{1}{2}x - 1$ oe	5	B2 for gradient 2 or M1 for $\frac{\pm (91)}{\pm (5 - 0)}$ or gradient of -2 AND M1 for ' <i>m</i> ' = $\frac{-1}{their2}$ B1 for $-\frac{1}{2}x - 1$, $y = -\frac{1}{2}x + c$ or $y = mx - 1$ or $y = (their m)x + c$ as answer	

	Ques	stion	Answer	Marks	Part marks ar	nd guidance
19			8.1 or 8.14	5	M1 for [vol sf] = 2400 ÷ 750 or 3.2 M1 for $\sqrt[3]{their 3.2}$ or 1.47 M1 for 12 ÷ their 1.47 A1 for 8.143 if A0 award B1 for their answer to at least 4 figures correctly rounded to 2 or 3 s.f.	Also 750÷2400 or 0.3125 $\sqrt[3]{their 0.3125}$ or 0.6786 12×their 0.6786 their 1.47 and their 0.6786 must be roots
20			20.9 or 20.89 or 20.886 or 21 with correct working	6	B1 for triangle AFB indicated e.g. drawn on diagram and M2 for [BF=] $\sqrt{(25^2 + 40^2)}$ or 47.16[9] or 47.17 or 47.2 or [AF=] $\sqrt{(25^2 + 40^2 + 18^2)}$ or 50.48 or 50.5 or M1 for $25^2 + 40^2$ [+18 ²] and M2 for e.g. tan ⁻¹ (18 ÷ <i>their</i> 47.169) or sin ⁻¹ (18 ÷ <i>their</i> 50.48) or M1 for [tan=] 18 ÷ <i>their</i> 47.169) or [sin=] 18 ÷ <i>their</i> 50.48)	<i>their</i> 47.169 should be an attempt at BF and <i>their</i> 50.48 should be an attempt at AF
21	(a)		[0].88 or [0].89 1.7[4]	2	B1 for each	
	(b)		Correct curve	2	B1 for 3 or 4 correct points plotted FT <i>their</i> table	tolerance $\pm \frac{1}{2}$ square
	(c)		2021 or 2022	2	B1 for <i>x</i> = 11 to 12	

	Question	Answer	Marks	Part marks ar	nd guidance
22		accept any correct method e.g. $P(R/M) = R = \frac{2}{5}$ $R = \frac{2}{5}$ $R = \frac{1}{4}$ $R = \frac{1}{4}$	B1	Could be table or the correct probability notation e.g. $P(R \cap M) = P(R/M) \times P(M)$	If they use a table see appendix based on 100 Award B3 for all red elements in table correct, B2 for 3 or 4 correct, B1 for 2 correct M1 for Prop.(F) = $25 \div 33.333$ or 0.75 M1 for Prop.(M) = $40 \div 66.666$ or 0.6
		$\frac{2}{3} \times P(R/M) = \frac{2}{5}$ $P(R/M) = \frac{2}{5} \div \frac{2}{3} = \frac{3}{5}$	M1 M1	Correct method to find the probability that a male is right-handed	
		$\frac{1}{3} \times P(R/F) = \frac{1}{4}$ P(R/F) = $\frac{1}{4} \div \frac{1}{3} = \frac{3}{4}$	M1 M1	Correct method to find the probability that a female is right-handed	
		$\frac{3}{4} = 0.75 > \frac{3}{5} = 0.6$	A1	Must be two figures which can be compared	

Mark Scheme

APPENDIX

Q22 tables based on 100 and 300.

	М	F	Total
R	40	25	65
L	26.6[6]	8.3[3]	35
Total	66.6[6]	33.3[3]	100

Accept 26.7 and 66.7

	М	F	Total
R	120	75	195
L	80	25	105
Total	200	100	300

PMT

OCR (Oxford Cambridge and RSA Examinations) The Triangle Building Shaftesbury Road Cambridge CB2 8EA

OCR Customer Contact Centre

Education and Learning

Telephone: 01223 553998 Facsimile: 01223 552627 Email: <u>general.qualifications@ocr.org.uk</u>

www.ocr.org.uk

For staff training purposes and as part of our quality assurance programme your call may be recorded or monitored

Oxford Cambridge and RSA Examinations is a Company Limited by Guarantee Registered in England Registered Office; The Triangle Building, Shaftesbury Road, Cambridge, CB2 8EA Registered Company Number: 3484466 OCR is an exempt Charity

OCR (Oxford Cambridge and RSA Examinations) Head office Telephone: 01223 552552 Facsimile: 01223 552553 Cambridge



© OCR 2018